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8 **Tax Policy and Investment**

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The first ship to arrive in St. Petersburg in 1701, a Dutch vessel, received from Peter the Great the privilege of paying no custom duties for the rest of its physical life—a concession which had the effect of prolonging the ship's life for almost a century—three or four times the normal span."<sup>1</sup>

Just as Peter the Great's tax amnesty spurred substantial maintenance investment in that Dutch ship, many governments have apparently believed that tax policy can be used as an instrument to alter firms' capital investment decisions. Indeed, investment tax credits (ITCs), special investment reserve funds, or accelerated depreciation allowances have been the rule rather than the exception in more developed countries since World War II. Against this backdrop, however, economists have generally struggled to find a significant impact of tax policy on investment.

The empirical economic literature on investment finds its early roots in the work of Aftalian (1909), Clark (1917), and Fisher (1930). Aftalian and Clark observed that business investment is highly correlated with changes in business output, providing support for the early "accelerationist" school, while Fisher's neoclassical theory argued for the importance of marginal conditions. At the risk of oversimplifying, the literature subsequently divided into two camps. One side argued that the accelerator model performed so well empirically that it should be adopted as the standard model; the other side looked to neoclassical models relating investment to the user cost of capital. The neoclassical school may have had the theoretical high ground, but empirical implementations of neoclassical models have been generally disappointing. Indeed, while the time-series evidence has always revealed that lags of output are highly correlated with investment, interest rates have provided only limited additional explanatory power.<sup>2</sup> The debate between these two schools provides a useful introduction to our review of the literature relating tax policy to investment. Many observers even recently (e.g., Clark 1993) have argued that tax policy likely does

not significantly affect investment, and the arguments inevitably harken back to the accelerationist debate.

Motivated by the hope that the simplest neoclassical models failed to explain investment fluctuations because they were too stylized, substantial energy was devoted to the task of extending these models to incorporate more realistic assumptions in the 1970s and early 1980s.<sup>3</sup> Chief among these was the incorporation of costs of adjusting the capital stock. According to these models, investment is forward looking and based on rational expectations of future variables. Because companies base their expectations of future variables in part on their observations of the past, researchers identified a link between lagged variables and current investment. Indeed, correlation of past output growth and future "fundamentals" could be used to rationalize a strong correlation between current investment and past values of the growth of output. When asked to explain the time-series movements of investment, however, these new models proved disappointing. Additional variables that were meant to capture the marginal cost or return to investment seemed to be of little use, over and above output, in predicting investment. Moreover, structural parameter estimates tended to be wildly implausible. It is at this point in the evolution of the literature that we begin this review.

### 8.1 Models of Investment in the Neoclassical Tradition

Models in the neoclassical tradition focus on the derived demand for capital by value-maximizing firms.<sup>4</sup> This intuition is typically transformed into models of investment by making assumptions about costs of changing the capital stock. For simplicity of exposition, consider the decisions of a price-taking firm. Absent taxes, in each period  $t$ , firm  $i$ 's real cash flow is given by

$$X_{i,t} = F(K_{i,t-1}, N_{i,t}) - w_t N_{i,t} - p_t I_{i,t} - C(I_{i,t}, K_{i,t-1}), \quad (8.1)$$

where  $K(\bullet)$  is the capital stock,  $F(\bullet)$  is the real revenue function of the firm,  $N$  is the variable factor,  $w$  is the price of the variable factor,  $p$  is the real price of investment goods, and  $C(\bullet)$  is the function determining the cost of adjusting the capital stock. In the absence of taxes, then, the marginal cost of newly installed capital is  $p_t + C_I(I_{i,t}, K_{i,t-1})$ .

To study investment tax policy, we add to the net cash flow expression (8.1) a profits tax at rate  $\tau$ , an investment tax credit at rate  $k$ , and the present value of a dollar's worth of depreciation allowances,  $z$ .<sup>5</sup> With

these additions, the marginal cost of newly installed capital is

$$p_t(1 - \Gamma_{i,t}) + (1 - \tau_t)C_I(I_{i,t}, K_{i,t-1}),$$

where  $\Gamma_{i,t} = k_t + \tau_t z_{i,t}$ , and we can rewrite equation 8.1 as:

$$X_{i,t} = (1 - \tau_t)(F(K_{i,t-1}, N_{i,t}) - w_t N_{i,t} - C_I(I_{i,t}, K_{i,t-1})) - p_t(1 - \Gamma_{i,t})I_{i,t}.$$

Under the assumption of value maximization, the firm maximizes the present value of its future net cash flows. Letting  $\beta$  be the discount factor appropriate for the  $i$ th firm, the firm's value at time  $t$  is given by

$$V_{i,t} = \max_{E_{i,t}} \sum_{s=t}^{\infty} \left( \prod_{j=t}^s \beta_{i,j} \right) X_{i,s}, \quad (8.2)$$

where  $E_{i,t}$  is the expectations operator for firm  $i$  conditional on information available at time  $t$ . The firm chooses the path of investment and employment of the variable factor, given the initial capital stock, to maximize firm value. The change in the capital stock—net investment—is given by  $I_{i,t} - \delta K_{i,t-1}$ , where  $\delta$  is the (assumed constant) proportional rate of depreciation.

For investment, the solution to the problem requires that the marginal value of an additional unit of investment equals its marginal cost. Denoting the shadow value of an additional unit of investment by  $q_t$ ,<sup>6</sup>

$$q_{i,t} = p_t(1 - \Gamma_{i,t}) + (1 - \tau_t)C_I(I_{i,t}, K_{i,t-1}). \quad (8.3)$$

The shadow price  $q$  must also obey

$$\Delta q_{i,t} = (\tau_{i,t} + \delta_t)q_{i,t} - (1 - \tau_t)F_K(K_{i,t-1}, N_{i,t}) + (1 - \delta_t)C_K(I_{i,t}, K_{i,t-1}), \quad (8.4)$$

where  $\tau$  is the instantaneous rate at which marginal cash flows are discounted.

We can now use this general setup to examine two conventional formulations of the neoclassical approach: one based on the user cost of capital and one based on  $q$ .

#### User Cost of Capital

Jorgenson (1963) and his collaborators suggested using a form of equation 8.4 to derive an expression for the user cost of capital. If we interpret  $q$  as the price at which a unit of capital can be bought or sold, we can consider the thought experiment of renting a unit of newly installed

capital. The owner of this capital will levy a rental cost  $c$  such that the rate of return equals  $r$ , the return available on alternative (financial) assets. The owner's return from renting the capital equals the rental cost,  $c$ , plus the capital gain on the machine,  $\Delta q_{i,t+1}/q_{i,t}$ , less the depreciation of the machine,  $\delta q_{i,t}$ . Expressed as a rate of return and equating the rate of return with the available alternative yields

$$c_{i,t} = \left( (1 - \tau_i)(r_{i,t} + \delta_i)q_{i,t} - \frac{\Delta q_{i,t}}{q_{i,t}} \right). \quad (8.5)$$

We can substitute for  $q$  in equation 8.3 to express the user cost as a function of the price of investment goods, adjustment costs, and tax parameters. Jorgenson assumed that adjustment costs were zero, yielding the familiar user cost expression:

$$c_{i,t} = p_t \left( \frac{1 - \Gamma_{i,t}}{1 - \tau_i} \right) \left( r_{i,t} + \delta_i - \frac{\Delta(p_{t+1}(1 - \Gamma_{i,t}))}{p_t(1 - \Gamma_{i,t})} \right). \quad (8.6)$$

Returning to our derivation of  $q$  in equation 8.3, we can more generally express the user cost as equaling the marginal cash flow of an additional unit of capital:

$$(1 - \tau_i)(F_K(K_{i,t-1}, N_{i,t}) - C_K(I_{i,t}, K_{i,t-1})) = c_{i,t}. \quad (8.7)$$

Jorgenson's interest centered on isolating the effects of the user cost on the desired capital stock and investment. He considered a special case in which the prices  $p$ ,  $w$ , and  $r$  are constant and  $I_{i,t} = \delta K_{i,t-1}$  in steady state (so that  $C_K = C_K = 0$ ). Hence from equation 8.7,

$$(1 - \tau_i)F_K(K_{i,t-1}, N_{i,t}) = c_{i,t}.$$

Assuming a constant elasticity of substitution production function,

$$F(K, N) = A[bK^{-\theta} + (1 - b)N^{-\theta}]^{-1/\theta},$$

where  $A > 0$ ,  $0 < b < 1$ , and  $\theta > -1$ , one can express the marginal revenue product of capital as

$$F_K(K, N) = \left( \frac{b}{A\theta} \right) \left( \frac{F}{K} \right)^{1+\theta}.$$

Returning to the Jorgensonian derivation in equation 8.7, the steady-state capital stock can be described as a function of the user cost of capital and

the firm's real revenue,

$$K^* = \left( \frac{b}{A\theta} \right)^\sigma F^\sigma \left( \frac{c}{1 - \tau} \right)^{-\sigma}, \quad (8.8)$$

where  $\sigma$  is the elasticity of substitution ( $\sigma = 1/(1 + \theta)$ ).

Equation 8.8 describes the steady-state capital stock,  $K^*$ . As we describe in more detail below, it is not an "estimating equation." To estimate investment, Jorgenson assumed that  $\sigma = 1$  (Cobb-Douglas technology), so that  $K^*_{i,t} = (b/A\theta)((1 - \tau_i)F_{i,t}/c_{i,t})$ . He then assumed that the capital stock adjusted to the desired level at an exogenous rate dictated by, say, delivery lags. A substantial empirical debate ensued, with Eisner and Nadiri (1964, 1970) claiming on the one hand that the elasticity of substitution is near zero than unity, while Jorgenson and Stephenson (1969) claimed on the other hand that an elasticity of unity is more consistent with the data.<sup>7</sup>

More contemporary applications of the user cost model incorporate explicit adjustment costs as opposed to ad hoc mechanisms such as delivery lags. Auerbach (1989), for example, begins with the Euler equation for investment and assumes a production function with productivity shocks and adjustment cost function. He approximates the optimal solution for perturbations by solving a linearized version of the Euler equation. He then derives a relationship between the investment rate ( $I_{i,t}/K_{i,t-1}$ ) and the user cost of capital, in which the user cost coefficient is a function of the steady-state average user cost and a root of the linearized difference equation in  $K$  (for applications, see Auerbach and Hassett 1991, 1992, and Cummins, Hassett, and Hubbard 1994, 1996).

### The $q$ Theory

Tobin's (1969)  $q$  theory of investment made more rigorous Keynes's (1936) idea that the incentive to add new fixed capital depends on the market value of capital relative to its replacement cost. Tobin represented by  $q$  the ratio of the market value of the firm to the replacement cost of the capital stock. One can easily incorporate adjustment costs and tax parameters in the  $q$  framework (see Hayashi 1982).

Returning to equation 8.2, we know that equilibrium marginal  $q$  is related to the price of investment goods, tax parameters, and adjustment costs. If we assume that the adjustment cost function is quadratic,

$$C(I_{i,t}, K_{i,t-1}) = \frac{\omega}{2} \left( \frac{I_{i,t}}{K_{i,t-1}} - \mu_i \right)^2 K_{i,t-1}, \quad (8.9)$$

where  $\mu$  is the steady-state rate of investment and  $\omega$  is the adjustment cost parameter, then equation 8.2 can be rewritten as an investment equation:

$$\frac{I_{it}}{K_{i,t-1}} = \mu_i + \frac{1}{\omega} \left[ \frac{q_{it} - p_i(1 - \Gamma_{i,t})}{(1 - \tau_i)} \right]. \quad (8.10)$$

Equation 8.10 offers a convenient way of estimating the responsiveness of investment to neoclassical variables, including tax parameters, but there is a hitch: marginal  $q$  is unobservable. Following Hayashi (1982), if the firm is a price taker in input and output markets and the production function exhibits constant returns to scale, marginal  $q$  equals average  $q$ , defined for each firm as tax-adjusted  $q$  (denoted below by  $Q$ ),

$$Q_{it} = \frac{V_{it} + B_{it} - A_{it}}{K_{i,t-1}^R}, \quad (8.11)$$

where  $V$  is the market value of the firm's equity,  $B$  is the market value of the firm's debt,  $A$  is the present value of depreciation allowances on investment made before period  $t$ , and  $K^R$  is the replacement value of the firm's capital stock (including inventories).

The  $Q$  formulation stresses a relationship between investment and the net profitability of investing, as measured by the difference between the value of an incremental unit of capital and the tax-inclusive cost of purchasing capital. As with the user cost approach, by making assumptions about costs of adjusting the capital stock, one can estimate effects of investment incentives on investment.

### Foreshadowing Empirical Problems

Jorgenson (1963) investigated whether a version of equation 8.8 could be used to describe aggregate fluctuations in U.S. investment. Moving from this equilibrium relationship to an empirical model, however, required a few more steps. Because output is determined by the choice of  $K$ , equation 8.8 does not relate  $K$  to a set of exogenous variables.<sup>8</sup> Rather, it expresses a relationship between endogenous variables that holds in equilibrium. Indeed, equation 8.8 does not define an investment relationship, that is, the *flow* of capital, but rather describes only the equilibrium *stock* of capital.<sup>9</sup> Jorgenson moved to an "investment" specification by defining a firm's "desired" capital stock,  $K^*$ , as  $Y/c$ , and then assuming that the firm gradually approached this desired stock over time. He assumed that the

rate at which the firm closed the gap between its actual and desired stock was given exogenously and did not affect the level of the "desired" stock. These assumptions yielded the estimating equation:

$$I_{it} = \sum_{j=0}^T w_j (K_{i,t-j} - K_{i,t-1-j}^*) + \delta K_{i,t-1}. \quad (8.12)$$

Hall and Jorgenson (1967) originally used such a model to explain aggregate investment and concluded that it described the data well. Eisner and his collaborators later pointed out that the model they estimated—recognizing that  $K^*$  was the ratio of output to the user cost—could be capturing accelerator effects, which had long been known to be strong explanatory factors for investment. In particular, if one constrained the user cost to be a constant, one could rewrite equation 8.12

$$I_{it} = \sum_{j=0}^T w_j (Y_{i,t-j} - Y_{i,t-1-j}) + \delta K_{i,t-1}, \quad (8.13)$$

which is a form of an accelerator model. When critics of Hall and Jorgenson isolated the separate contribution of the user cost to explaining investment, they found it to be negligible (see Eisner 1969, 1970; Eisner and Nadin 1968; Chirinko and Eisner 1983).

Nonetheless, by the late 1960s, the neoclassical model developed by Jorgenson and others had become the standard model for studying investment decisions, but empirical debates remained. On the one hand, the neoclassical approach offered a structural link between tax policy parameters—the corporate tax rate, the present value of depreciation allowances and the investment tax credit—and investment through the user cost capital.<sup>10</sup> On the other hand, the empirical evidence suggested that the more rigorous theory did not improve the econometrician's ability to explain aggregate investment fluctuations or the response of business investment to changes in tax policy.

Partially in response to this empirical concern, models based on the representation of the firm's investment problem occupied much of the empirical research by the 1980s.<sup>11</sup> A key appeal of the  $Q$  approach was that it related investment to a variable that was (under certain assumptions) easier to observe than the user cost of capital. However, empirical adaptation of  $Q$  models did not fare well in explaining either time-series or cross-sectional (firm-level) variation in investment.

Despite such empirical frustrations, policymakers in the United States and other industrial economies, given the frequency with which the

manipulate tax policy parameters, evidently believe that business fixed investment responds to tax changes. Hence it is disturbing that models emphasizing the net return to investing are defeated in forecasting "horse races" by ad hoc models and that structural variables are frequently found to be economically or statistically insignificant.<sup>12</sup> Recently the investment literature has begun to make a convincing case that the fundamentals are in fact key determinants of investment but that they appear to have little effect in the macro data because of several severe econometric problems.<sup>13</sup> To set the stage for the discussion of these problems in section 8.3, we first review key stylized facts about the time-series behavior of business fixed investment and "fundamental determinants of investment."

### 8.2 Some Stylized Facts About Business Fixed Investment

In figure 8.1, we plot aggregate U.S. equipment investment against several investment fundamentals. The top panel shows the comovement of investment and the Jorgensonian user cost. The series rarely move together in an obvious way, and the correlation since 1960 is a statistically insignificant -.11. The second panel illustrates the strong comovements between investment and corporate cash flow. The two series are roughly coincident, and the correlation over time is a highly significant .64. The bottom panel illustrates the accelerator effect, which relates changes in the growth rates of output and equipment spending. As with cash flow, the correlation is large and highly significant, and the coincidence of the series is visually striking.

Although one should be cautious interpreting such correlations formally, they nonetheless suggest clear patterns. Aggregate equipment investment varies significantly over the business cycle and neither lags nor leads the cycle; it is highly correlated with other variables that are also highly procyclical. The time-series correlation between investment and the user cost, on the other hand, is quite weak. Figure 8.1 can be thought of as a visual summary of the early investment literature: accelerator effects are strong and obvious; user cost effects appear weaker and more subtle.

We focus on studies of equipment investment in structures have been more disappointing. Figure 8.2, which repeats figure 8.1 with the relevant fundamentals related to the growth rate of investment in nonresidential structures, illustrates the problem. Structures investment is less clearly correlated with all of the fundamentals. The correlation with the user cost is insignificant and has the incorrect sign, the correlation with cash flow is

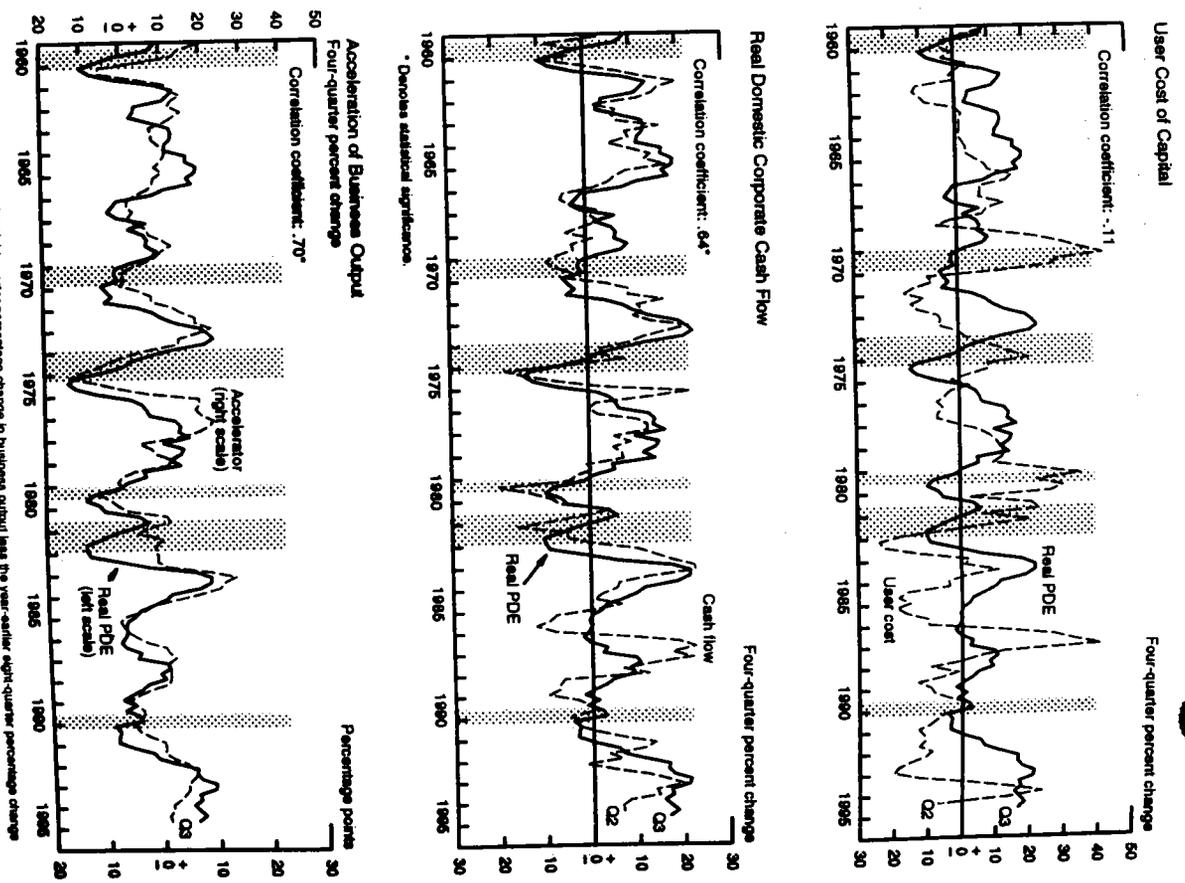


Figure 8.1  
Fundamental determinants of equipment spending. Source: Bureau of Economic Analysis (BEA).

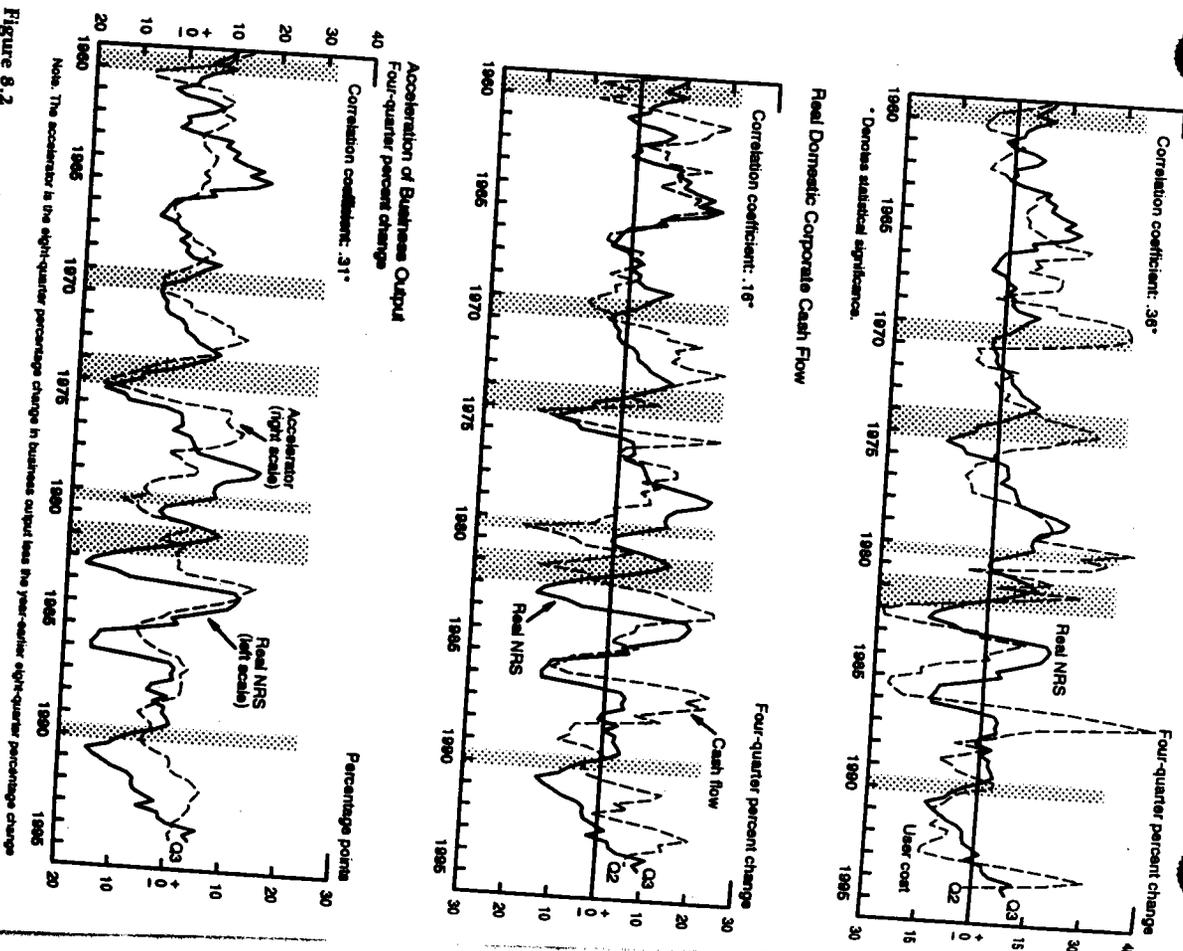


Figure 8.2  
Fundamental determinants of nonresidential structures (NRS) spending. Source: BEA.

about one-fourth of that between cash flow and equipment investment, and the accelerator effect, still noticeable, is significantly weaker.

An alternative branch of the investment literature has followed the suggestion of Tobin (1969) that investment should be related to  $Q$ , the ratio of the market value of the firm to the replacement costs of its capital stock. Figure 8.3 depicts the correlation of aggregate business fixed investment with  $Q$ .<sup>14</sup> The top panel compares the level of real investment to the level of  $Q$ . Clearly the low-frequency movements in the two series are not highly correlated. The bottom panel relates the growth rates of these two series. Here it appears that growth in  $Q$  leads growth in investment somewhat, although the relationship is weak, and the contemporaneous correlation is actually negative.<sup>15</sup>

To summarize, the tendency for a number of aggregate variables to move together over the business cycle makes it difficult to isolate effects of individual fundamentals on investment. Hence a partial equilibrium investment demand approach might have very little power to explain aggregate investment fluctuations. Movements of the aggregate variables, including investment, are determined simultaneously, and disentangling the marginal impact of a single driving variable is difficult, if not impossible. For example, suppose that aggregate demand increases exogenously for some reason. This shift might lead firms to be more optimistic about their sales prospects and to purchase more investment goods: it might also be expected, at least in the short run, to lead to higher interest rates. If we then examine the correlation between investment and the interest rate, we might even find that the sign is the opposite of that predicted by the theory. While an instrumental variables procedure might allow us to overcome this simultaneity problem, the estimator is only as good as the instruments, and it is difficult to imagine an appropriate set of instruments for this application. Microeconomic data, however, provide a rich additional source of variation, and it is to the microdata studies that we now turn.

### 8.3 Estimating Effects of Tax Policy on Investment Using Microdata

Standard investment models emphasizing the net return to investment yield four empirical representations, each beginning with the firm maximizing its net present value. The first-order conditions lead to a Euler equation describing the period-to-period optimal path of investment. Abel

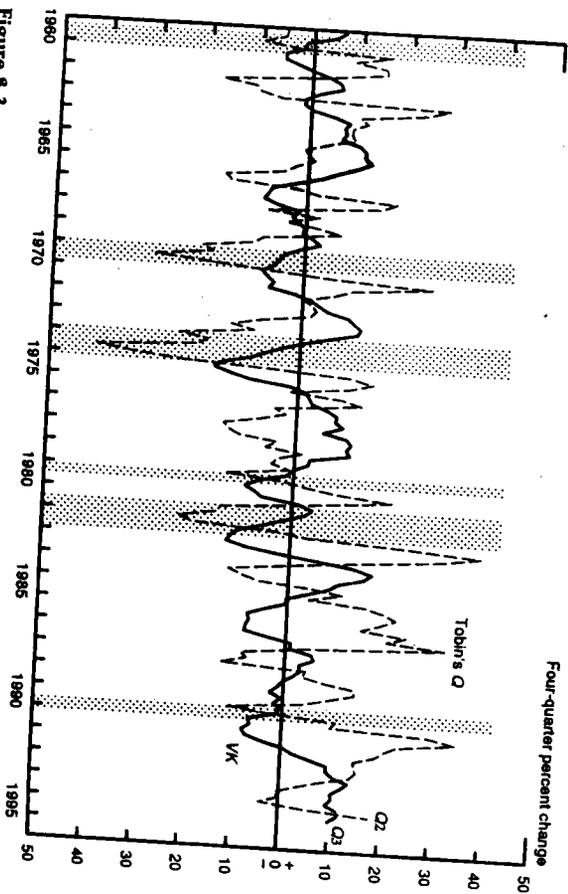
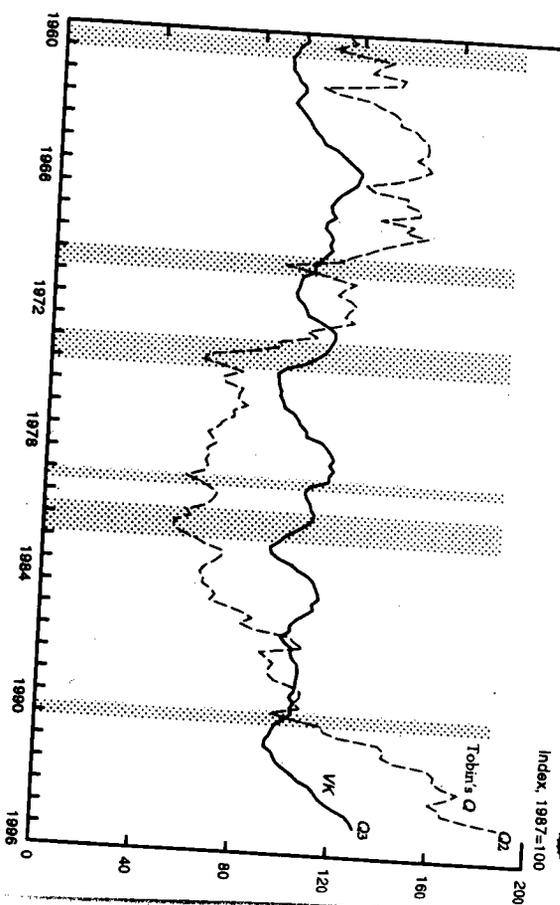


Figure 8.3  
Tobin's Q and the I/K ratio. Source: BEA and Federal Reserve, Flow of Funds.

and Blanchard (1986) solved the difference equation that relates investment to its expected current and future marginal revenue products of capital, Gilchrist and Himmelberg (1995) apply a related forecasting approach to panel data. Alternatively, effects of tax parameters may be estimated from the Euler equation (see, e.g., Abel 1980; Hubbard and Kashyap 1992). As in Auerbach (1983b) and Abel (1990), investment can be expressed in terms of current and future values of the user cost of capital and, under some conditions, expressed in terms of average  $q$ . Again, this approach was suggested initially by Tobin (1969), with the necessary conditions supplied by Hayashi (1982).

**The Basic Problem**

To assess recent empirical work on tax policy and investment, we begin with the following general model of investment, which follows the discussion in section 8.1:

$$\frac{I_t}{K_{t-1}} = S_t \gamma + \varepsilon_t \quad (8.14)$$

where  $I$  and  $K$  denote investment and the capital stock, respectively;  $S$  is an underlying structural variable (e.g., the expected value of tax-adjusted  $Q$  or the user cost of capital) or set of variables;  $\gamma$  is a coefficient whose structural interpretation relates to assumptions about convex costs of adjusting the capital stock; and  $\varepsilon$  is a white-noise error term that reflects optimization error by firms.<sup>16</sup>

Researchers usually estimated such models using either ordinary least squares or generalized method of moments techniques with instrumental variables. Cummins, Hassett, and Hubbard (1994, 1996) note that conventional estimated values of  $\gamma$  in firm-level panel data for the United States or for other countries are very small, ranging from 0.01 to 0.05, implying marginal costs of adjustment of between one and five dollars per dollar of investment. Such estimates, which have emerged in many empirical studies (Summers 1981; Salingier and Summers 1983; Fazzari, Hubbard, and Petersen 1988a), imply very small effects of permanent investment incentives on investment.

Subsequently, empirical researchers have offered two general explanations of the failure to estimate significant tax effects on investment: (1) measurement error in fundamental variables and (2) misspecification of costs of adjusting the capital stock. Both research programs have contributed

our understanding of the responsiveness of investment to changes in the net return to investing and have reached similar conclusions about the likely effects of tax policy for some important cases.

### *Measurement Error in Fundamental Variables*

A major problem in using equation 8.14 in order to recover estimates of marginal adjustment costs and the effect of tax changes on investment is that measurement error in  $Q$  or the user cost of capital may bias downward the estimated coefficient. A number of techniques have been suggested to address this measurement error, including statistical corrections, avoiding the use of  $Q$  or user cost representations, using new proxies for  $Q$  focusing on periods or frequencies in which firm variation in fundamental variables is less subject to measurement error, and modifying assumptions about the financial frictions firms face. We consider each in turn and examine whether the techniques produce a consensus estimate of adjustment costs that can be used to forecast the effects of investment incentives on business fixed investment.

### **Statistical Approaches**

There are at least two problems in measuring  $Q$  that might affect estimated adjustment costs. First, to the extent that the stock market is excessively volatile,  $Q$  might not reflect market fundamentals. Second, the replacement value of the capital stock in the denominator of  $Q$  is likely to be measured with error. Giliches and Hausman (1986) argue that measurement error will lead to different biases among potential estimators that are similar in that they control for firm-specific effects but differ in their signal-to-noise ratios, making it possible to place bounds on the importance of measurement error. Cummins, Hassett, and Hubbard (1994) estimate a model like equation 8.14 using first differences and longer differences (as opposed to the conventional fixed-effects, within-group estimator) to address measurement error problems. Their estimated adjustment costs decline significantly.

In a time-series setting, Caballero (1994) pursues an alternative estimation strategy, based on a suggestion by Stock and Watson (1993). Caballero argues that small sample biases of typically employed time-series estimation procedures are particularly severe when estimating adjustment cost models, and he shows that elasticities will generally be biased downward. Using the procedure of Stock and Watson for estimating the

low-frequency relationships between variables in small samples, Caballero estimates a long-run elasticity of investment with respect to the user cost of approximately unity. This is much larger than the early estimates, but roughly consistent with the other studies summarized in this section.

### **Euler Equation Estimates**

The second approach departs from the strategy of using proxies for marginal  $q$  and relies on the firm's Euler equation to model the investment decision. (As long as one makes the same assumption about technology and adjustment costs, the Euler equation can be derived from the same model as the conventional  $Q$  or user cost of capital models.) By not relying on the "investment function" representation, one can sidestep problems of measuring marginal  $q$ .

Tests following this approach have frequently used panel data on manufacturing firms to estimate the Euler equation (Pindyck and Rotemberg 1983; Shapiro 1986; Gilchrist 1991; Whited 1992; Bond and Meghir 1994; Hubbard, Kashyap, and Whited 1995). Studies using Compustat data for the United States are unable to reject the frictionless neoclassical model for most firms, and the estimated adjustment cost parameters are more reasonable than those found in estimates of  $Q$  models. For example, Hubbard, Kashyap, and Whited (1995) report estimated values of  $\gamma$  between 1 and 2.2. Very similar estimates are reported for European manufacturing firms by Cummins, Harris, and Hassett (1995) and for investment in overseas subsidiaries of U.S. multinational corporations in Cummins and Hubbard (1995).

### **Alternatives to $Q$**

The measure of average  $Q$  used as a proxy for marginal  $q$  in most empirical studies is constructed as the ratio of the market value of the financial claims on the firm (equity and debt) to the replacement cost of the firm's capital stock. The third approach bypasses using financial variables as proxies for marginal  $q$  by forecasting the expected present value of the current and future profits generated by an incremental unit of capital—that is, the expected value of marginal  $q$ —an idea developed (in the time-series context) by Abel and Blanchard (1986) and extended for use in panel data by Gilchrist and Himmelberg (1995). One can extend this setup to a panel-data setting by constructing investment fundamentals using a VAR forecasting framework to decompose the effect of profits or cash flow on investment into two components: one that forecasts future profitability under the frictionless capital markets assumed in the neoclassical model

(analogous to marginal  $q$ ) and a residual component that may be attributable to financial frictions (analogous to the role played by cash flow in the imperfect-capital-markets approach of Fazzari, Hubbard, and Petersen 1988a). By including lags of cash flow in the vector of observed fundamentals in the forecasting equations, one can ensure that any information about future marginal profitability of capital contained in cash flow is reflected in the proxy for marginal  $q$ .

Using such an approach, Gilchrist and Himmelberg (1995) report estimates of  $\gamma$  that are roughly consistent with the Euler equation estimates discussed above. In addition, they test whether cash flow is an independent "fundamental" variable explaining investment and find that it is for a subset of firms that are likely to face financing constraints.<sup>17</sup> (We return to a discussion of this latter result below.)

### Measuring Changes in Fundamentals Using Tax Reforms

One reason the data do not appear to favor neoclassical models over accelerator models is a simultaneous equations problem. If the data are dominated by exogenous increases or decreases in the real interest rate, then the user cost movements would lead investment to decrease or increase, respectively. But if investment rises with positive "animal spirits," then higher investment demand puts upward pressure on the real interest rate. Hence to the extent that data incorporate exogenous changes in both the real interest rate and the intercept of the investment function, the positive relationship between investment and the user cost of capital because of shifts in the investment function may dominate the hypothesized negative relationship between investment and the user cost of capital. In this case, the estimated coefficient on the user cost of capital will be "too small," leading to estimated adjustment costs that are "too large." Such simultaneity increases apparent accelerator effects, because positive shifts in the investment function raise both investment and output.

This simultaneity problem in the estimation of neoclassical models is remedied by the use of instrumental variables. Conventional instrumental variables (including lagged endogenous variables or sales-to-capital ratios) have not proved very helpful. Major tax reforms arguably offer periods in which there is exogenous cross-sectional variation in the user cost of capital or tax-adjusted  $q$ . Cummins, Hassett, and Hubbard (1994, 1996) demonstrate that major tax reforms are also associated with significant firm- and asset-level variation in key tax parameters (such as the effective rate of investment tax credit and the present value of depreciation allow-

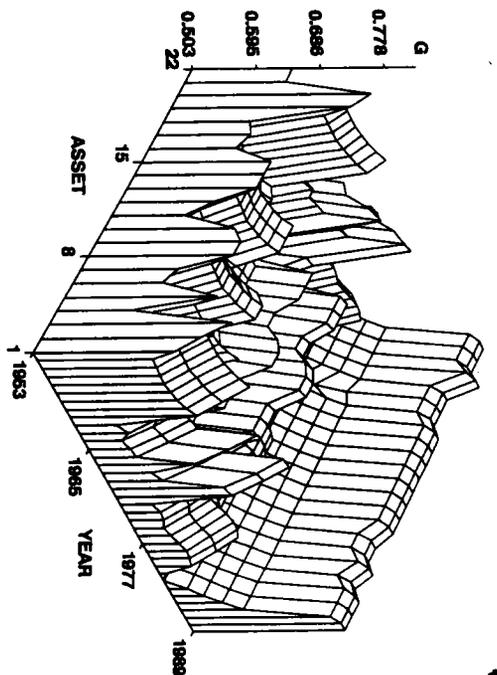


Figure 8.4  
After-tax cost of one dollar of equipment investment, 1953–1989. Source: Author's calculations based on data from the BEA.

ances). Hence tax variables are likely to be a good instrument for the user cost or  $Q$  during tax reforms.

To indicate the significance of cross-sectional heterogeneity in incentives to invest, we emphasize variation across assets. Figure 8.4 plots the annual values of  $(1 - T)$  for the twenty-two classes of equipment capital classified by the Bureau of Economic Analysis (BEA). The peaks and valleys along the year axis for a given asset reveal the time-series variation in the tax parameters, and those along the asset axis for a given year reveal the cross-sectional variation. For asset 8 (metalworking machinery), for example, the after-tax cost of investing falls in 1962, 1972, and 1981 and rises in 1986.

Figure 8.4 reveals that the variation across assets is large within most years in our samples, as is the time-series variation. In addition, the positions of the peaks and valleys change somewhat over time. For example, following the removal of the investment tax credit and the reduction of the corporate tax rate by the Tax Reform Act of 1986, the cross-sectional variation across assets fell, consistent with the act's stated goal to "level the playing field."

Cummins, Hassett, and Hubbard (1995) use vector autoregressions to forecast investment in the year following a tax reform and then compare the forecast errors for each of the assets to the changes in the user cost for

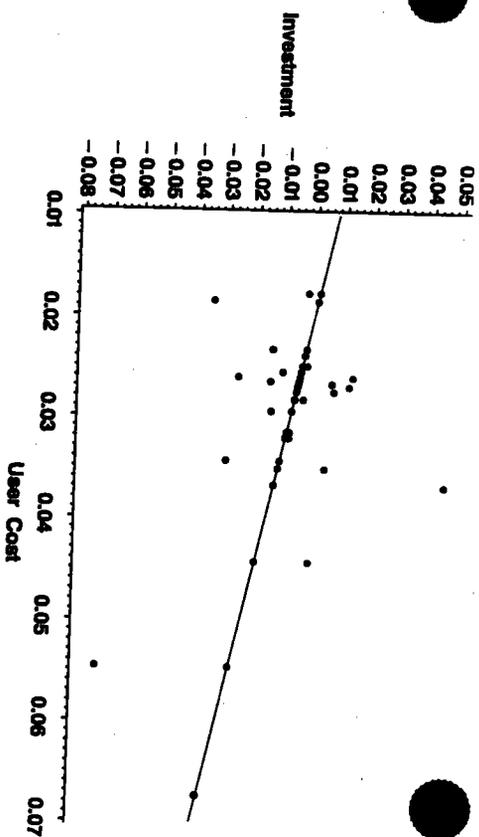


Figure 8.5  
Cross-sectional relationship between investment and user cost forecast errors, 1987. Source: Cummins, Hassett, and Hubbard (1994, figure 3).

that asset. In figure 8.5, we repeat that experiment and for the Tax Reform Act of 1986, and provide a plot of the forecast errors constructed from models that exclude taxes against shocks to the user cost of capital for each of the twenty-two equipment asset classes tracked by the BEA. In addition, we draw a regression line through the scatterplot. The idea is that the forecast errors for investment should be negatively correlated with forecast errors for the user cost of capital. The downward-sloping line indicates a clear negative correlation.

We can now illustrate the effect of tax parameters on firm investment. Table 8.1 shows the significance of using exogenous tax changes to identify changes in  $Q_{1t}$ . Taken from Cummins, Hassett, and Hubbard (1996), it presents estimates of the investment equation (8.14) during major tax reforms in fourteen countries over the 1980s; firm-level data are taken from Compustat's Global Vantage. Using contemporaneous tax variables as instrument during major tax reforms, Cummins, Hassett, and Hubbard estimate  $\gamma$  to be 0.65 for the United States, compared with 0.048 under conventional estimates. They obtained similar estimates for each of the other major U.S. tax reforms in the postwar period using data from Compustat (Cummins, Hassett, and Hubbard 1994); focusing on the Tax Reform Act of 1986, Auerbach and Hassett (1991) found similar coefficients using asset-level data and cross-sectional variation in the user cost.

Table 8.1  
Estimates of tax-adjusted  $Q$  model for fourteen countries

Country	Conventional panel data estimated coefficient on $Q^a$	Estimated coefficient with contemporaneous tax instruments
Australia	0.050 (0.019)	0.289 (0.153)
Belgium	0.103 (0.044)	0.587 (0.422)
Canada	0.041 (0.009)	0.521 (0.127)
Denmark	0.104 (0.085)	0.765 (0.308)
France	0.085 (0.042)	0.388 (0.116)
Germany	0.095 (0.040)	0.784 (0.296)
Italy	0.051 (0.018)	0.180 (0.120)
Japan	0.029 (0.008)	0.086 (0.035)
The Netherlands	0.069 (0.044)	0.633 (0.150)
Norway	0.069 (0.031)	0.512 (0.295)
Spain	0.044 (0.028)	0.404 (0.233)
Sweden	0.051 (0.047)	0.293 (0.169)
United Kingdom	0.062 (0.013)	0.589 (0.078)
United States	0.048 (0.006)	0.650 (0.077)

Source: Calculations in Cummins, Hassett, and Hubbard (1996) using Global Vantage data.  
<sup>a</sup>See table 5 in Cummins, Hassett, and Hubbard (1996), GMM estimates. Instruments include twice- and thrice-lagged values of  $Q(I/K)$ , and the ratios of cash flow to capital.  
<sup>b</sup>See table 7 in Cummins, Hassett, and Hubbard (1996), GMM estimates. Instruments include twice- and thrice-lagged values of  $I/K$  and the ratio of cash flow to capital, twice-lagged value nontax components of  $q$ , and contemporaneous values of tax parameters.

As table 8.1 shows, applying the Cummins-Hassett-Hubbard approach in tax reform periods in other Organization for Economic Cooperation and Development countries produces estimates roughly similar to those for the United States.<sup>19</sup>

### Financial Frictions and the Neoclassical Model

In contrast to the frictionless capital markets in the standard neoclassical model, earlier applied research on investment, especially the work of Meyer and Kuh (1957), stressed the significance of financial considerations (particularly internal funds or net worth) for business investment. Since the mid-1960s, however, most applied research on investment isolated "real" firm decisions from "financing." The intellectual justification for this shift in approach drew on the seminal work by Modigliani and Miller (1958), who demonstrated the irrelevance of financial structure and financial policy for real investment decisions under certain conditions. The central Modigliani-Miller result, which facilitated the early development of the neoclassical model, was that a firm's financial structure will not affect its value in frictionless capital markets. As a result, if their assumptions are satisfied, real firm decisions, motivated by the maximization of shareholders' claims, are independent of financial factors such as the availability of internal funds.

The assumption of representative firms (in terms of trade on capital markets) is common to most research programs in the neoclassical tradition. That is, the same empirical model (e.g., equation 8.14) applies to all firms. Therefore, tests could not ascertain whether the observed sensitivity of investment to financial variables differs across firms and whether these differences in sensitivity explain the weak apparent relationship between the measured user cost and investment. Contemporary empirical studies of information and incentive problems in the investment process have moved beyond the assumption of representative firms by examining firm-level panel data in which firms can be grouped into high-net-worth and low-net-worth categories. For the latter category, changes in net worth or internal funds affect investment, holding constant underlying investment opportunities (desired investment).<sup>20</sup> Following Fazzari, Hubbard, and Petersen (1988a), empirical researchers have placed firms into groups as a priori financially constrained or financially unconstrained.

Two aspects of the findings of this research program are noteworthy in the context of measuring incentives to invest. First, numerous empirical studies have found that proxies for internal funds have explanatory power for investment, holding constant  $Q$ , the user cost, or accelerator variables

(see the review of studies in Hubbard 1996). This suggests that tax policy may have effects on investment by constrained firms beyond those predicted by neoclassical approaches. (Indeed, returning to the accelerator analogy, Bernanke, Gertler, and Gilchrist 1996 argue that this literature describes a financial accelerator.) In particular, the quantity of internal funds available for investment is supported by the average tax on earnings from existing projects. In this sense, average as well as marginal tax rates faced by a firm affect its investment decisions.<sup>21</sup>

Second, empirical studies of financing constraints generally find that the frictionless neoclassical model is rejected only for the groups of firms that a priori are financially constrained (Calomiris and Hubbard 1995; Gilchrist and Himmelberg 1995; Hubbard, Kashyap, and Whited 1995). Hence, while the shadow value of internal funds may not be well captured for some firms in standard representations of the neoclassical approach, the neoclassical model with convex adjustment costs yields reasonable estimated values of marginal adjustment costs for most firms.

### Measurement Error and Adjustment Costs: Nearing Consensus?

To summarize, a variety of empirical implementations of the neoclassical model with convex adjustment costs have attempted to mitigate measurement error and other econometric problems in conventional ordinary least squares and generalized method of moments (GMM) estimates of equation 8.14 in panel data. For  $Q$  models, the methods described generally yield estimated values of  $\gamma$  of .50 or higher, implying marginal costs of adjustment in the range of ten cents per dollar of additional investment (using the estimate in Cummins, Hassett, and Hubbard 1994 as a benchmark), and elasticities of investment with respect to the user cost of capital between  $-0.5$  and  $-1.0$ .

### An Alternative Interpretation: Misspecification of Adjustment Costs

The emphasis in many recent empirical studies of investment on sources of mismeasurement of explanatory variables acting as proxies for the net return to investing accepts the conventional belief that costs of adjusting the capital stock are convex. The  $Q$ , user cost of capital, and Euler equation approaches can all be derived from the same intertemporal maximization problem, given common assumptions about technology, competition, and adjustment costs. An important recent line of inquiry focuses on modeling and testing the effects of irreversibility and uncertainty on firms' investment decisions (see the excellent survey by Dixit and Pindyck 1994).<sup>22</sup>

this literature is correct, then there may be important regions wherein tax policy has little or no effect on investment, and knowledge of which region an economy is in is an important prerequisite to any policy analysis. Finally, these models can possibly explain a key remaining puzzle in the literature: why firms report in surveys that they use such high hurdle rates (Summers 1987).

Neoclassical models implicitly assume that there is an efficient secondary market for capital; hence irreversibility poses no problem. If a firm purchases a machine today and the output market turns sour in the future, the firm can recoup the purchase price of the machine at that time. But if investment is irreversible, the firm faces the chance that it cannot sell the machine in the future. In this setup, there is a gain to delaying investment and allowing the random price process to move either into a region far enough above the neoclassical "breakeven" point that the probability of the "bad state" becomes low enough, or into a region where it clearly does not make sense to purchase the machine. An investment extinguishes the value of the call option of delay, an option that has positive value when prices are uncertain. In this approach, the value of the lost option is a component of the opportunity cost of investment. In the terminology of the  $Q$  framework, the threshold criterion for investment requires that marginal  $Q$  exceed unity by the value of maintaining the call option to invest. As a consequence, high hurdle rates may be required by corporate managers who are making investment decisions.

Indeed, at least part of the interest in option-based investment models have been the problem raised in many time-series studies that indicated that the response of investment to changes in  $Q$  or the user cost of capital are implausibly small, implying, perhaps, that there are regions wherein  $Q$  varies but investment does not. In addition, it is not difficult to suggest examples of nonconvex adjustment costs, such as retooling in automobile plants or adopting more energy-efficient kilns in cement plants.

#### How Much Investment Is Irreversible?

Before turning to models with alternative adjustment cost specifications, we present a *prima facie* case that pure irreversibility may not be of overriding importance at the aggregate level.

A large literature (Hulten and Wykoff 1979; Jorgenson 1994; Fraumeni 1995; Oliner 1996) focuses on the estimation of economic depreciation rates for different types of machines. For the most part, researchers estimate rates of decay from the patterns of used machine prices. This literature is relevant to the debate concerning the form of adjustment costs

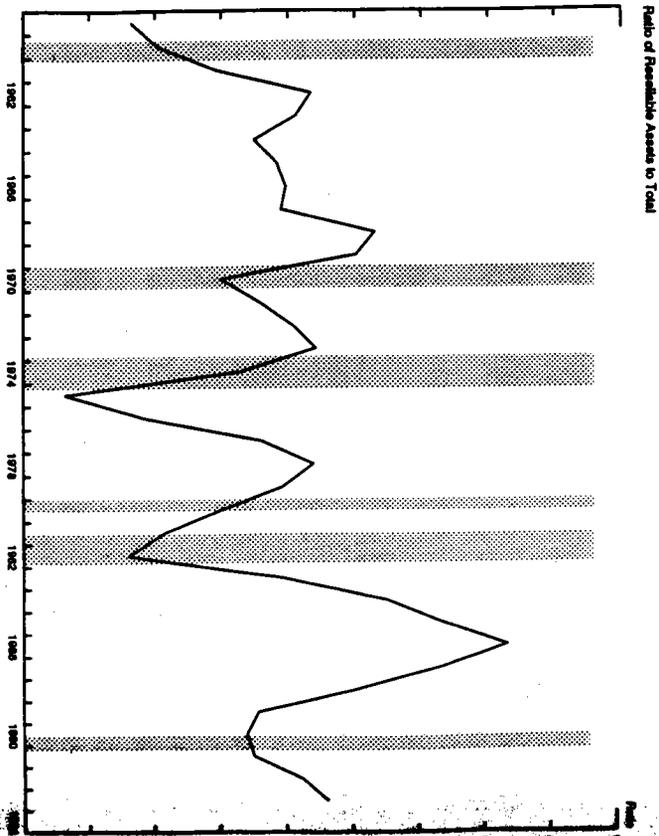


Figure 8.6  
U.S. equipment investment. Source: Author's calculations based on data from the BEA.

because irreversibility results most plausibly from either the absence of resale markets or the presence of significant "lemons" problems in resale markets.

To examine the extent to which resale markets are limited, we surveyed the depreciation literature and cataloged types of equipment for which we could find an estimated economic depreciation rate. Using disaggregated data on investment by asset type, we then calculated the proportion of aggregate investment that is made up of assets with clearly identifiable resale markets. Figure 8.6 plots this proportion from 1960 to 1994. The proportion of investment in assets that have easily identifiable resale markets is about 0.7 over most of the period. This is not to say that the remaining assets are necessarily irreversible; of course, depreciation studies may not yet have found data for those assets.

Hence, in order to demonstrate that irreversibility is an important property of most investment goods, researchers must show that the market for used capital goods is plagued with lemons problems. To our

knowledge, there is no existing evidence that lemons are important in markets for equipment goods. Indeed, Hulthen and Wyckoff (1981) argue that estimated secondary market prices in depreciation studies are inconsistent with a major role for lemons problems. One reason for this finding may be that the market for used capital good is one where the participants possess significant asset-specific expertise. The typical purchaser of a machine tool, for example, may have worked in a factory filled with machine tools for many years and would easily recognize a lemon. If this is the case, there is little asymmetric information, and the resale market functions well.

### Models with More General Adjustment Costs

Abel and Eberly (1994) provide a general framework that encompasses irreversibility, fixed costs, and a wide array of alternative adjustment cost specifications. They show that, under certain conditions, the investment behavior of firms can be characterized by three distinct regimes: a regime in which gross investment is (1) positive, (2) zero, or (3) negative. The responsiveness of investment to fundamentals differs across regimes, and their more general model predicts a region in which gross investment will stay zero for a range of unfavorable values of  $Q$ . Because this model nests the more traditional  $q$  models, it provides a useful empirical framework, and we review attempts to estimate this model below.

Researchers are beginning to study the impact of alternative adjustment cost assumptions within structural investment models with panel data. Barnett and Sakellaris (1995) use Compustat data to investigate the implication of the model of Abel and Eberly (1995) that investment alternates between regimes of insensitivity to  $Q$  and regimes of responsiveness to  $Q$ . The region of inactivity should be close to the region for which the model predicts that investment is negative. Because the thresholds for these regions are unknown, conventional asymptotic distributions do not apply. Barnett and Sakellaris use a statistical framework that allows them to estimate the threshold points and the coefficients on  $Q$  simultaneously in the different regions given the threshold points. They find evidence of a nonlinear relationship between investment and  $Q$ ; in particular, they estimate the largest responsiveness of investment to  $Q$  for low values of  $Q$  and the smallest for very high values of  $Q$ . On average, they estimate that the elasticity of investment with respect to  $Q$  is about unity but that the aggregate elasticity varies considerably over time, depending on the average level of  $Q$ . Barnett and Sakellaris argue that their results imply that adjustment costs may not be quadratic, though the most likely cause

is not firms' inability to disinvest but, rather, their reluctance to make large changes.

Barnett and Sakellaris's results are not necessarily inconsistent with the measurement error story. Some firms in the Compustat universe have values of average  $Q$  that are astronomical (one firm actually has a  $Q$  of 40,000), presumably because the capital stock measure is missing important goodwill or human capital components. If one accepts that  $Q$  is a poor measure of fundamentals for these firms, then the result that investment does not respond as much to  $Q$  for these firms is not surprising. In the more normal range of  $Q$  values, the investment response seems to accord well with the predictions of the convex adjustment cost model.

Using firm-level data from Compustat, Abel and Eberly (1996a) estimate that the relationship between investment and fundamental determinants ( $Q$  and the tax-adjusted price of capital goods) is concave; that is, the response of investment to fundamental determinants is positive but monotonically declining. The results of Abel and Eberly suggest that the distribution of tax-adjusted  $Q$  or the user cost of capital may be a determinant of aggregate investment. However, the caution that applied to Barnett and Sakellaris conclusions applies here as well: large, observed values of  $Q$  may not coincide with high levels of investment because the high  $Q$  values reflect mismeasurement rather than extraordinary fundamentals.

Finally, Caballero, Engel, and Haltiwanger (1995) explore adjustment costs in a more general framework. Using a subset of 7,000 U.S. manufacturing plants from the Census Bureau's Longitudinal Research Database (LRD), they explore whether cross-sectional patterns of investment are consistent with symmetric, convex adjustment cost models or whether the data imply nonconvexities.<sup>23</sup> They proceed in two steps. First, they assume that there are no adjustment costs and that the Jorgenson model adequately describes a firm's "desired" capital stock ( $K^*$ ).<sup>24</sup> They then compare in each period a firm's beginning-of-period capital stock to its desired stock and call the difference ( $K^* - K_{t-1}$ ) "mandated investment." Second, they explore how firms actually adjust their capital stock. In this step, they find that the relationship between actual and mandated investment is highly nonlinear. If mandated investment is negative, firms do not quickly adjust their capital stocks downward. If mandated investment is small and positive, then firms also do not respond much. If mandated investment is very large, firms adjust their capital stocks quickly. They conclude that an ( $S, s$ ) model, in which firms have a range of inaction and adjust their capital stocks to their desired level only when the gap between current and desired capital stock is "enough" offers a good description of the data.

Caballero, Engel, and Haltiwanger also illustrate how to construct aggregate implications from their microeconomic results. Integrating over the microeconomic distribution of plants, they calculate a predicted aggregate elasticity of investment with respect to the user cost of capital. The estimates of this elasticity vary considerably over time. If many plants are near the region for which mandated investment is very large, then small changes in the user cost can have large effects on aggregate investment. If, however, the bulk of the distribution of mandated investment is in the region of low responsiveness of investment to fundamentals, then changes in the user cost will have little impact. They concur with the main conclusion of Cummins, Hassett, and Hubbard (1994) that the aggregate elasticity of investment with respect to the user cost is between  $-0.5$  and  $-1$ , and also conclude that tax reforms appear to have had generally large effects on investment. They caution, however, that the reforms have had large effects because they coincidentally occurred during periods in which the plant-level distribution of mandated investment was aligned in such a way to allow a large effect of changes in tax parameters. This would happen if, for example, investment tax credits were removed in booms, when mandated investment is very large, and an increase in the user cost can cause firms to cancel significant investment plans. As a consequence, Caballero, Engel, and Haltiwanger argue that researchers must consult the microdistribution of mandated investment before predicting the likely impact of future tax reforms on business investment.<sup>25</sup>

Alternatively, Cummins, Hassett, and Hubbard (1994, 1996) argue that recovering "reasonable" estimates of the response of investment to  $Q$  or the user cost of capital is easiest when large exogenous changes in the distribution of structural determinants occur, as during tax reforms. In response to the alternative interpretation that firms respond to changes in fundamentals only when these changes are large, Cummins, Hassett, and Hubbard use firm-level data to investigate whether there was evidence of bunching of investment around tax reforms. They estimate transition probabilities among various ranges of  $I/K$  over the year prior to, of, and after the tax reform and find no evidence that firms with large investment were likely to have lower investment in prior or subsequent years. Indeed, only a very tiny fraction of the sample was ever found to transit from high investment to low investment states.

In part, the conclusions of these studies may differ because of differences in the level of aggregation. At a sufficiently fine level of disaggregation, all investment looks lumpy. The plant-level evidence suggests that investment appears lumpy, but the firm-level evidence does not corroborate

this. However, there may be interesting differences between the investment behavior of plants and firms, as might be the case if, for example, managerial attention is limited and only a fraction of a firm's plants adjust their capital in a given year. Clearly, reconciling the plant-level and firm-level results is an important topic for future research.

#### **Summing Up: The Partial Equilibrium Effects of Investment Tax Policy**

Recent studies appear to have reached a consensus that the elasticity of investment with respect to the user cost of capital is between  $-0.5$  and  $-1.0$ . Indeed, recent studies using convex costs of adjustment and studies using nonconvex costs of adjustments agree that the long-run elasticity of investment to the user cost is high by the standards of the early empirical literature. This range of estimated responses of investment to tax parameters is well above the consensus of only a few years ago and suggests that investment tax policy can have a significant impact on the path of aggregate capital formation. One should be cautious, however, in moving from the microeconomic evidence to aggregate predictions. Caballero, Engel, and Haltiwanger demonstrate a technique for aggregating the microdistribution of firms to calculate aggregate investment demand, but very little continues to be known about the general equilibrium effects of major policy changes.

#### **8.4 Arguments For and Against Investment Incentives**

Thus far we have argued that tax incentives for investment are important components of the net return to investing and the short-term and long-term responses of investment to permanent tax incentives are large. We now turn to the deeper policy question of whether we should have permanent incentives for investment even if such incentives increase the stock of business fixed capital. (We then address the question of the desirability of short-run incentives.) Economists generally argue against intervention. Under what circumstances might one advocate distortionary investment incentives?

#### **Do Investment Incentives Affect the Price of Capital Goods?**

One scenario under which investment incentives might have an especially large impact on the quantity of investment without dissipation in prices

of investment goods is one in which firms' demand for capital is responsive to changes in the user cost of capital and in which capital goods are supplied perfectly elastically. While it is implausible that the supply function for most individual capital goods manufacturers is perfectly elastic, the effective supply of capital goods to a given domestic market might well be highly elastic in the long run if the world market for capital goods is open. Investment incentives would raise prices of capital goods in the short run if the supply of capital goods is highly inelastic.

Using data for the United States and ten other countries, Hassett and Hubbard (1995) find that local investment tax credits have a negligible effect on prices paid for capital goods—indeed, they find that the capital goods prices for most countries are very highly correlated and that the movements of these over time are consistent with the "law of one price." In addition, using disaggregated data on asset-specific investment good prices and tax variables for the United States, they find that tax parameters have no effect on capital goods prices.<sup>26</sup> The conclusion that tax policy in the United States does not affect the world price of capital goods is especially meaningful, given the relative size of the U.S. economy. Taken together, these tests suggest that the effects of investment tax policy have not been muted in a significant way by upward-sloping supply schedules for capital goods.

### *Is the Capital Stock Too Small?*

While it is instructive to ask how effective investment incentives are at increasing the fixed capital stock, a more important question remains: What is the social value of the increase in the fixed capital stock?

Theoretical research has demonstrated that perfectly competitive economies do not necessarily converge to the "correct" capital stock. Indeed, Diamond (1965) demonstrated that a competitive economy can reach a steady state in which there is "too much" capital, in the sense that the economy is investing more than it is earning in profit. In this case, individuals can be made better off if they are forced to consume a portion of the capital stock. When evaluating investment incentives, it is crucial for policy analysis to evaluate whether the economy is operating with "too much" or "too little" capital.

The classic "golden rule" literature offers benchmarks for guidance.<sup>27</sup> In the golden rule approach of Phelps (1961), the golden rule level of the capital stock relative to output is achieved when the marginal product of capital ( $R$ ), net of depreciation ( $\delta$ ), equals the sum of the rate of growth of

the labor force ( $n$ ) and the rate of labor-augmenting technical change ( $g$ ), or:

$$R = \delta + n + g. \quad (8.15)$$

Alternatively, in the optimal growth literature, Ramsey's (1928) golden rule levels require that the marginal product of capital net of depreciation equal the sum of the social rate of time preference ( $\rho$ ) and the elasticity of marginal social utility with respect to per capita consumption ( $\phi$ ) or,<sup>28</sup>

$$R = \delta + \rho + \phi g. \quad (8.16)$$

Depending on the values of  $\rho$  and  $\phi$ , the Ramsey golden rule levels of capital can be less than the Phelps golden rule levels.

Following the convention in neoclassical models of the capital stock, we assume a Cobb-Douglas technology, so that the ratio of the steady-state golden rule capital stock ( $K^*$ ) to output ( $Y$ ) equals the ratio of capital's share in output ( $\alpha$ ) to the marginal product of capital ( $R$ ). Moreover, the golden rule level of net investment ( $I^*$ ) relative to output equals  $(n + g)$  times the capital output ratio. Hence:

$$\frac{K^*}{Y} = \frac{\alpha}{R} \quad (8.17)$$

and

$$\frac{I^*}{Y} = (n + g) \frac{K^*}{Y}. \quad (8.18)$$

One can account for different types of capital by noting that, in equilibrium, the net rates of return on the alternative types are equal. Hence one can substitute into equation 8.17 measure of  $\alpha_k$  for each type of capital  $k$  and the relevant  $R$  (given differences in depreciation), and solve for the golden rule levels of the capital stocks.

Using a range of parameter values in the golden rule expressions in equations 8.17 and 8.18, Cohen, Hassett, and Kennedy (1995) compare golden rule and actual levels of the capital stock and net investment relative to output to their actual values over the period from 1980 to 1994. Table 8.2, which we excerpt from several tables in that study, indicates that for benchmark parameter values, equipment investment and capital stocks are below their golden rule levels (assuming 1980–1994 is sufficiently long to characterize a steady state), while residential investment and the residential capital stocks, which received significant tax subsidies over this time period, are near or above their golden rule levels. Cohen

**Table 8.2**  
Benchmark golden rule and actual levels of  $I^{GR}/Y$  and  $K/Y$

Type of capital	Golden rule level		Actual level (1980-1994 average)
	Phelps	Ramsey	
Net investment as a percentage of GDP			
Total fixed	8.3%	6.0%	4.2%
Business fixed	4.8	3.6	2.4
Producers' durable	2.4	2.0	1.3
equipment			
Nonresidential	2.0	1.3	1.2
structures			
Residential	2.7	1.6	1.8
Ratio of capital stock to GDP			
Total fixed	3.3	2.4	1.9
Business fixed	1.9	1.4	1.0
Producers' durable	1.0	0.8	0.5
equipment			
Nonresidential	0.8	0.5	0.5
structures			
Residential	1.1	0.6	0.9

Source: Cohen, Hassett, and Kennedy (1995, Table 2).

Note: Benchmark parameter values are: labor force growth rate = 0.01; rate of labor-augmenting technical change = 0.15; social discount rate = 0.12; and social intertemporal elasticity of substitution ( $\Phi$ ) = 3.

<sup>a</sup>Total fixed = 0.30; <sup>b</sup>Business fixed = 0.24; <sup>c</sup>Equipment = 0.18; <sup>d</sup>Structures = 0.06; <sup>e</sup>Residential = 0.06.

Hassett and Kennedy also show that these conclusions are not changed if the key parameters are allowed to vary across a broad range of plausible values.

Alternatively, several authors have attempted to evaluate the optimality of the U.S. capital stock by relating various interest rates to the rate of economic growth. One the one hand, Tobin (1965), Solow (1970), and Feldstein (1977) argue that the marginal productivity of capital one obtains from accounting profits estimates is about 10 percent, and thus they conclude that the economy is dynamically efficient. On the other hand, Ibbotson (1987) calculates a mean return on U.S. Treasury bills from 1926 to 1986 of only 0.3 percent, suggesting dynamic inefficiency. The answer to the question using interest rates depends critically on assessing the impact of risk, of course.

Abel et al. (1989) pursue an alternative strategy for evaluating whether the U.S. capital stock is greater or less than the optimal level. In a stochastic

setting with a very general production technology, they demonstrate that an economy is dynamically inefficient if it invests more than the returns from capital. They show that the economy is dynamically efficient—and hence in the range in which stimulative tax policy might have positive social returns—if the returns from capital exceed investment. Using their terminology, the key questions is whether the capital stock is, on balance, a “sink” or a “spout.” This observation is a useful contribution because it allows one to base judgment about dynamic efficiency on readily observable cash flows. Abel et al. conclude that the economy is dynamically efficient. Thus, both capital stock data and cash flow data suggest that, by raising the stock of equipment capital, investment incentives have positive social returns.<sup>29</sup>

### *Should We Use Temporary Investment Incentives?*

The discussion thus far pertains to permanent changes in investment incentives. Even a casual observation of the history of investment incentives since the 1950s suggests the usefulness of considering temporary investment incentives. Since 1962, the mean duration of a typical state in which an ITC is in effect has been about three and one-half years, and the mean duration of the “no-ITC” state has been about the same length. In 1992, President Bush advocated a modified ITC, known as the Investment Tax Allowance, and President Clinton proposed an incremental ITC in early 1993; neither of these measures was enacted. What is the likely impact on aggregate capital accumulation of temporary investment incentives?

Temporary investment incentives can have even larger short-run impacts on investment than permanent investment incentives (Auerbach, 1989). Consider a temporary ITC known to last for one period. The expressions for the user cost of capital in equation 8.5 indicates that the ITC lowers the current user cost through both its effect on  $T_t$  and the consequences of its removal on  $T_{t+1}$ . More generally, anticipated future changes in tax policy affect the current value of the user cost of investment.

The large potential effects of temporary tax incentives on investment do not imply that they are desirable tax policy—even if one believes that long-run investment incentives are sound tax policy. In the presence of uncertainty and adjustment costs, there is little reason to believe that policymakers can time investment incentives for the purposes of capitalization policy. Moreover, the use of temporary incentives increas-

uncertainty in business capital budgeting, making it more difficult for firms to forecast the path of the user cost of capital.

### *Does Uncertainty About Tax Policy Affect Investment?*

What if firms do not know the exact timing of changes in investment incentives—that is, if tax policy is uncertain? A substantial literature evaluates the effects of price uncertainty on investment, and the lesson from this literature is that the sign of the effect of uncertainty on investment depends crucially on assumptions about adjustment costs and returns to scale. Hartman (1972) shows that uncertainty generally increases investment in a model with constant returns and convex adjustment costs. Abel (1983) derives a similar result in continuous time. Pindyck (1988), however, shows that uncertainty can significantly lower capital formation if investment is irreversible and returns to scale are decreasing. We described Pindyck's intuition earlier: in an uncertain world, there is a gain to delaying investment—the option value of waiting—and these gains are higher the higher is the variance in the output price.

Thus, one might be tempted to conclude from the early contributions to this literature that the predicted effect of tax policy uncertainty will depend on what we believe about the reversibility—or lack thereof—of capital investments. However, strictly speaking, tax policy uncertainty can increase investment in the models of Hartman, Abel, and even Pindyck (see Hassett and Metcalfe 1994, 1995).

This difference arises because tax policy uncertainty is unlike price uncertainty in an important way. Researchers often introduced uncertainty by assuming that the price follows a continuous-time random walk (Brownian motion or geometric Brownian motion). When prices follow a random walk, the appropriate rational expectations forecast for the price at any time in the future is today's price, and the future path of the price is unbounded. Unlike most prices, tax parameters tend to remain constant for a few years and then jump to new values. In addition, jumps in the ITC tend to be mean reverting: when the credit is high, it is likely to be reduced in the future, and when the credit is low, it is likely to be increased in the future. Because of these properties, the normal gain to waiting in a model with irreversibility is reduced significantly when an investment tax credit is "on". Because the firm fears that the credit might be eliminated, it is more likely to invest today while the credit is still effective. Hassett and Metcalfe demonstrate that this effect dominates the reverse effect in the state in which there is no investment tax credit, and

they conclude that increasing tax policy uncertainty raises aggregate investment.

As with the case of temporary investment incentives generally, this result does not imply that random tax policy is desirable. Most existing studies analyze investment in a partial equilibrium setting wherein there are no utility costs to bunching capital formation. In a general equilibrium setting, Bizer and Judd (1989) show that welfare is reduced significantly by random investment tax policy. The randomness has a negative impact because consumers wish to smooth consumption, and fluctuations in investment credits make smoothing costly.

### **8.5 Policy Implications**

Our finding of significant short-term and long-term effects of the user cost of capital on equipment investment suggests applications to current policy debates. In particular, we evaluate consequences for the user cost and investment of a reduction in inflation and a switch from an income tax to a broad-based consumption tax.

#### *Low Inflation as a "Costless" Investment Subsidy*

Many economists (see e.g., Feldstein 1976; King and Fullerton 1984) have argued that under fairly general assumptions, a reduction in the rate of inflation provides a relatively costless stimulus to business fixed investment by reducing the user cost of capital. Returning to the expression for the user cost, there are two channels through which expected inflation affects investment decisions. First, for given values of  $r$  and  $\delta$ , the user cost varies positively with the level of expected inflation  $\pi$  because the present value of depreciation allowances—which is formed using the nominal rate,  $r + \pi$ , as a discount rate—varies inversely with inflation owing to historical-cost depreciation.<sup>30</sup> Second, inflation affects the real cost of funds,  $r$ . In this section, we briefly illustrate this second channel (following Auerbach 1983b) and calculate the extent to which lower inflation over the past decade led to a reduction in the user cost of capital.

In a small open economy, the real cost of debt would be determined in world capital markets and would be exogenously given to firms. If the capital market were closed, the marginal tax rate of the holder of debt would affect the interest rates that firms pay. That is, local debt holders

require a fixed real after-tax return,  $r$ , where

$$r = i(1 - \tau_p) - \pi, \quad (8.19)$$

where  $i$  is the nominal interest rate on corporate debt,  $\tau_p$  is the marginal personal tax rate on interest income, and  $\pi$  is the expected rate of inflation. The inflation premium component of interest income is taxable to bondholders. The firm's real cost of debt,  $\rho_d$ , depends on its own marginal income tax rate,  $\tau_c$

$$\rho_d = i(1 - \tau_c) - \pi, \quad (8.20)$$

because under current U.S. tax law, nominal interest payments on corporate debt are fully deductible. Combining the two previous expressions relates the firm's, real cost of debt to the investor's required return and marginal tax rate:

$$\rho_d = (r + \pi) \frac{(1 - \tau_c)}{(1 - \tau_p)} - \pi. \quad (8.21)$$

Alternatively,

$$\rho_d = \frac{r(1 - \tau_c) + (\tau_p - \tau_c)\pi}{(1 - \tau_p)}. \quad (8.22)$$

The firm's real cost of equity finance,  $\rho_e$ , is defined as

$$\rho_e = D + E - \pi, \quad (8.23)$$

where  $D$  is the dividend-price ratio and  $E$  is investor's required ex-dividend nominal return to equity.

Note that for a given  $r$ , inflation has very little effect on the cost of debt finance if—as is likely the case in the United States— $\tau_c$  is approximately equal to  $\tau_p$ . In this case, lower inflation reduces the nominal interest deduction but lowers the tax liability of bondholder by the same amount. Note also that the effects of inflation on the cost of debt finance depend crucially on the assumption that the marginal debt holder is taxable. If the marginal debt holder is a pension fund (whose income is not taxed under current law), then lower inflation unambiguously increases the cost of debt finance. Firms receive smaller interest deductions, and pension funds do not accrue an offsetting reduction in tax liability.<sup>31</sup>

Individuals receive the after-tax real return,

$$\rho_i = (1 - \tau_i)D + (1 - c)E - \pi, \quad (8.24)$$

where  $\tau_i$  is the individual's marginal tax rate on dividend income and  $c$  is the individual's accrual equivalent tax rate on capital gains. Combining terms, the firm's real cost of equity finance is

$$\rho_e = \frac{(1 - c)}{(1 - c)} D + \frac{\rho_i}{(1 - c)} + \frac{c}{(1 - c)} \pi. \quad (8.25)$$

Higher inflation unambiguously increases the cost of equity finance by the factor  $c/(1 - c)$ . This term captures the "inflation tax" paid by shareholders who receive purely nominal gains; taxation of real capital gains would eliminate this effect.<sup>32</sup>

The total real cost of investment funds is simply the weighted average of the cost of equity and the cost of debt, where the weights are the share of each in marginal finance. Using this approach, one can examine the effect on investment of recent declines in expected inflation. Cohen, Hassett, and Hubbard (1996) calculate the marginal effects on the user cost of lowering inflation.<sup>33</sup> They estimate that under plausible assumptions, the current value of the user cost for equipment investment is about 0.22, and they conclude that a one-percentage-point permanent decrease in inflation lowers the user cost by about one-half a percentage point. In their calculations, the incremental effect of each additional percentage point reduction in inflation is approximately the same. Thus, if the annual inflation rate were reduced from 4 percent to zero, the user cost of capital would decline about two percentage points—proportionally by about 10 percent. Given the elasticity estimates reviewed in the previous section, this "tax cut" would provide a significant stimulus to investment.

### Moving to a Consumption Tax

Under the income tax, the user cost of capital is influenced by the corporate tax rate, investment tax credits, and the present value of depreciation allowances (see equation 8.6). Under a broad-based consumption tax firms pay tax on the difference between receipts and purchases from other firms. That is, there is no investor's tax credit, and investment is expensed ( $z = 1$ ). In this case (assuming that the corporate tax rate does not change over time), the user cost of capital simplifies to

$$c_{it} = p_t \left[ r_t + \delta_t - \frac{\Delta p_{t+1}}{p_t} \right]. \quad (8.26)$$

Comparing the user cost expressions in equations 8.6 and 8.6' leads to two observations. First, under a consumption tax, taxes do not dist-

business investment decisions: investment decisions are based on nontax fundamentals. Second, given current U.S. tax policy, the user cost is lower under a consumption tax than under an income tax.

By how much? Under current law, and assuming that the output price and the capital goods price are both equal to unity, then for assets with seven-year lives (assuming that the expected real interest rate is 4 percent, the expected inflation rate is 3 percent, and the marginal machine is financed half with equity and half with debt), the value of  $(1 - \Gamma)/(1 - \tau)$  under 1996 U.S. tax law is 1.148, and the user cost of capital is equal to 0.234. The move to the consumption tax would lower the value of the user cost to 0.205, a reduction that would lead, *ceteris paribus*, to about a 10 percent increase in equipment investment given the consensus estimates of  $\gamma$  in equation 8.14.

Of course, other aggregate variables are also likely to change if such a large change to the tax code were adopted. For example, nominal interest rates and the supply of savings are likely to change. While it is difficult to say how large the net stimulus to investment would be, the consensus of the recent investment literature suggests that the partial equilibrium impact on investment may be quite large.

## 8.6 Conclusions

Economists and policymakers have long been concerned about the effects of business taxation and investment incentives on the equilibrium capital stock and the timing of investment. Such concerns figure prominently in research programs (1) identifying impacts of tax parameters on fundamental determinants of investment, (2) describing links between fundamentals and the capital stock or investment, and (3) testing models of those links. Studies within the neoclassical tradition offer rigorous applications of the first two, but until recently have not produced reasonable empirical estimates of effects of fundamentals on investment. Indeed, the empirical estimates of effects of neoclassical factors led some researchers to conclude that "taxes don't matter" and still others to question assumptions of the neoclassical paradigm.

Our principal conclusions are four. First, neoclassical models that use convex costs of adjusting the capital stock to derive investment equations yield economically important short-run and long-run effects of tax policy on investment. This result reflects recent research that, through a number of complementary approaches, demonstrates that measurement error in fundamentals biases downward conventional estimates of tax effects. Sec-

ond, at least for data on firm-level investment, predictions of models with nonconvex adjustment costs are no more consistent with observed links between fundamentals and investment than those of models with convex adjustment costs. Third, recent studies conclude that U.S. business investment is below its golden rule level. Finally, consensus estimates of the impact of the user cost of capital on investment indicate that two current policy suggestions—pursuing a monetary policy that would reduce expected inflation and switching from an income tax to a consumption tax—would significantly stimulate investment.

The current state of research on business investment decisions suggests the desirability of developing tests to distinguish among alternative models of costs of adjusting the capital stock. Different adjustment cost specifications imply different time paths of the response of the capital stock to tax policy, making such tests useful for policymakers. Nonetheless, most recent studies imply a high long-run elasticity of the capital stock to the user cost of capital, so that tax policy clearly has the potential to have a powerful effect on equipment investment and the capital stock in the long run.

## Notes

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1. See Braudel (1992, p. 241).
2. We update the time-series stylized facts in section 8.2.
3. Eisner and Strotz (1963) offer an early discussion of adjustment costs. The theory was developed and extended by Lucas (1967, 1976), Gould (1966), Treadway (1969, 1973), Uzawa (1969), Mortensen (1973), Abel (1980), and Hayashi (1982). Researchers have generally assumed convex costs of adjusting the capital stock—the idea that it is more costly to implement a given increment to the capital stock quickly rather than gradually. We discuss alternative assumptions about adjustment costs in section 8.4.
4. For a more detailed discussion of the models introduced in this section, see Auerbach (1990).
5. For the sake of simplifying the discussion, we focus here on the U.S. tax system. For a parallel analysis that employs a more general tax formulation nesting that of many countries, see Sinn (1987) and King and Fullerton (1984). Sweden, in particular, has had one of the more complicated and interesting tax codes in the postwar period. For a discussion relating its code to this model, see Taylor (1982), Södersten (1989), and Auerbach, Hassett, and Södersten (1995).

6. Implicit in this derivation is the idea that firms can remove capital goods and sell them subject to an adjustment cost.
7. It may be important to allow the ex ante and ex post values of  $\sigma$  to be different, the argument being that the labor needed for a given piece of capital in place is fixed. This is the "putty-day" hypothesis, put forward by Bischoff (1971). In some cases, these models have been shown to perform well empirically (see Strudmeyer 1983).
8. To be more specific, Jorgenson assumed that the revenue function of the firm was Cobb-Douglas and that the firm set marginal revenue (with respect to capital) equal to the user cost in order to maximize profits.
9. For example, Haavelmo (1960) writes, "The demand for investment cannot simply be derived from the demand for capital.... I think the sooner this naive, and unfounded theory of the demand for investment schedule is abandoned, the sooner we shall have a chance of making some real progress in constructing more powerful theories to deal with the capricious short-run variations in the rate of private investment" (quoted in Jorgenson 1967, p. 133).
10. In an alternative representation, Feldstein (1982) explored the effects of effective tax rates on investment in reduced-form models; for a critique of this approach, see Chirinko (1987).
11. As we noted earlier, Hayashi (1982) provided the conditions required to equate marginal  $q$  with average  $Q$  which is observable because it depends on the market valuation of the firm's assets. Summers (1981) incorporated additional tax parameters in the  $Q$  model.
12. See e.g., Bosworth (1985), Bernanke, Bohn, and Reiss (1988), and the survey in Chirinko (1993). The often poor empirical performance of  $Q$  models has led some researchers to abandon the assumptions of reversible investment and convex costs used in testing neoclassical models in favor of approaches based on lumpy and "irreversible" investment. See e.g., the discussions and reviews of studies in Pindyck (1991), Dixit and Pindyck (1994), and Hubbard (1994).
13. Taylor (1993) does find, however, that aggregate fixed investment is significantly negatively related to the real interest rate in every one of the Group of 7 countries.
14. The measure of  $Q$  plotted here is constructed from data from the Federal Reserve's Flow of Funds Accounts.
15. If we regress the growth rate of business fixed investment on many lags of the growth rate of  $Q$ , the sum of the coefficients is about 0.1, implying that a 20 percent increase in the rate of  $Q$  would lead to a prediction of about a 2 percent higher growth rate of business fixed investment. Cochrane (1991) finds significantly larger effects of the growth of  $Q$  on the growth of total private investment. The results differ because Cochrane's measure of investment includes residential investment, which is—perhaps surprisingly—more highly correlated with stock market fluctuations.
16. One could, of course, incorporate more complex error structures. We make this simplifying assumption for ease of exposition.
17. This is a test of the restricted model against the alternative model that current profits have explanatory power for investment beyond their ability to predict future profits. Gilchrist and Hurnelberg find that cash flow is an independent fundamental and that excess sensitivity of investment to cash flow is a characteristic of firms they identify as constrained—measured by size, bond rating, commercial paper rating, or dividend payout.

18. Cummins, Hassett, and Hubbard (1994, 1995) also use this approach in a user cost model. For U.S. data, they estimate a user cost coefficient of about -0.65.
19. Tax reforms are not the only plausible reform that can be used to estimate adjustment costs. A large body of evidence suggests that union power to expropriate returns is significant and that the "union tax" adjusts as the return to capital changes. If union wage demands vary with the return to capital, then the union rent share is—in part at least—a tax on capital, distorting the level of investment when it is introduced. Fallick and Hassett (1995) explore whether a change in the union status of the firm is another type of large, identifiable shock that affects purchases of capital. Using firm-level panel data, they document a large negative response of investment to union certification elections. For most of the firms that experience union certification elections in their sample, net investment turns significantly negative in the year immediately following the election, with the mean response to union certification being roughly the same size as that which would occur—given the responsiveness of investment to the user cost in Cummins, Hassett, and Hubbard (1994)—if the corporate tax rate were increased by 35 percentage points. This set of firms, at least, is not burdened by an ability to adjust their capital stock downward when a negative shock to profitability occurs.
20. For reviews of the theoretical literature, see Bernanke, Gertler, and Gilchrist (1996) and Hubbard (1990, 1996).
21. Fazzari, Hubbard, and Petersen (1988b) and Gertler and Hubbard (1988) illustrate this point in examining the effect of the investment tax credit on investment. Calomiris and Hubbard (1995) focus on a tax experiment in which retained earnings are taxed more heavily than distributed profits. In frictionless capital markets, firms would take advantage of the incentive to change their payout policies. Working against this response for some firms is the potential difference in the cost of internal and external funds. To the extent that the marginal cost of external funds is high, a growing firm with profitable investment opportunities might choose to pay the undistributed profits tax and invest its internal funds rather than distribute funds and then reacquire them in the capital market. The U.S. undistributed profits tax of 1936-1937, which imposed a graduated surtax on corporate retention, offers a useful experiment. Because the maximum marginal tax rate on corporate retention was 27 percent, most firms had large incentives to alter their payout policies. Using firm-level panel data from the 1930s, Calomiris and Hubbard find that a neoclassical investment model with no explicit capital market frictions is rejected only for firms with high ex ante surtax margins.
22. The seeds of this literature are much older. For example, Rothschild (1971) writes: "Convex cost-of-adjustment functions may help to explain why Rome was not built in a day. However, there is no clear saving and may be some loss to spreading the work of installing a button on a shirt over several weeks." His "bang-bang" model of investment provides an early example of a "lumpy investment" model.
23. In earlier work, Doms and Dunne (1994) report that plant-level investment data exhibit skewness and kurtosis that is consistent with investment's being somewhat lumpy.
24. To calculate the desired capital stock for each firm, Caballero, Engel, and Haltiwanger use plant-level output data and two-digit Jorgensonian user costs constructed from the tax data used in Cummins, Hassett, and Hubbard (1994) and Goolsbee (1996).
25. Because their mandated investment measure is the same as that in a frictionless neoclassical model, their tests, although suggestive, neither confirm nor reject the presence of convex adjustment costs. First, mandated investment itself depends on adjustment costs. Second, if adjustment costs were present, mandated investment also depends on future values of tax parameters.

26. Using a different approach, Goolsbee (1996) finds evidence that U.S. tax shocks are positively correlated with capital price movements. He argues that the elasticity of investment demand with respect to the user cost is likely greater than unity (in absolute value), but that an upward-sloping short-run supply curve for capital goods likely dampens mildly the effects of tax policy.

27. Another argument for subsidies to equipment investment has been advanced by Judd (1995), who concludes that the optimal tax on equipment investment is negative. He argues that to the extent that capital-goods-producing industries are imperfectly competitive (owing, say, to the presence of patents), equipment prices contain significant markups. Hence to return firm's input mix to the optimal level, the government should design an investment subsidy that equates the price paid for equipment to its marginal cost.

28. See, e.g., the analysis in Blanchard and Fischer (1989).

29. Because the golden rule models are developed for a closed economy, it is difficult to extend the comparison to domestic versus foreign fixed capital.

30. That is, the present value of depreciation allowances is given by:

$$\sum_{t=1}^{\infty} (1+r_t + \alpha_t) \tau DEP_t (s-f),$$

where  $DEP_t(a)$  is the depreciation allowance permitted an asset of age  $a$ , discounted at a nominal rate that includes the expected inflation rate  $\pi$ .

31. There is no clear consensus regarding the effects of marginal tax rates on domestic real interest rates or on the question of whether the "Fisher effect" implicit in equation 8.21 holds. This is an important area for future research in this context.

32. For the calculations described below, we do not include the first term reflecting the tax on dividends. In effect, we adopt the "tax capitalization" view of equity taxation (summarized in Auerbach 1983b), which suggests that the relevant tax rate is the effective capital gains tax rate, regardless of the amount of dividends paid. This view assumes that marginal equity funds come primarily from retained earnings rather than from new share issues and that earnings distributions to shareholders are primarily through dividends rather than share repurchases.

33. Earlier empirical studies of the effect of inflation on real business tax burdens include Feldstein and Summers (1979) and Auerbach (1983b). Cohen, Hassett, and Hubbard (1996) also allow for inflation to increase taxes paid because of the effects of inflation on the cost of carrying inventories.

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